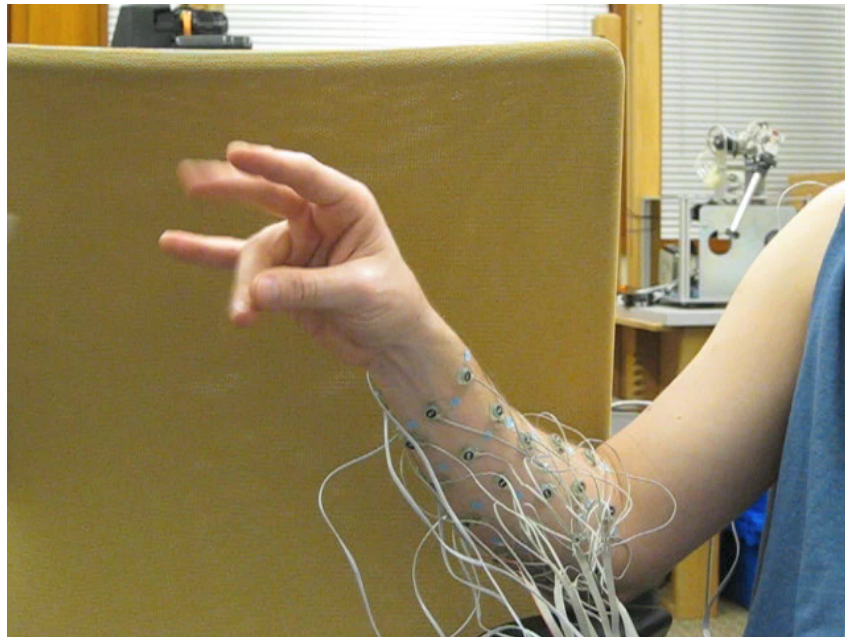
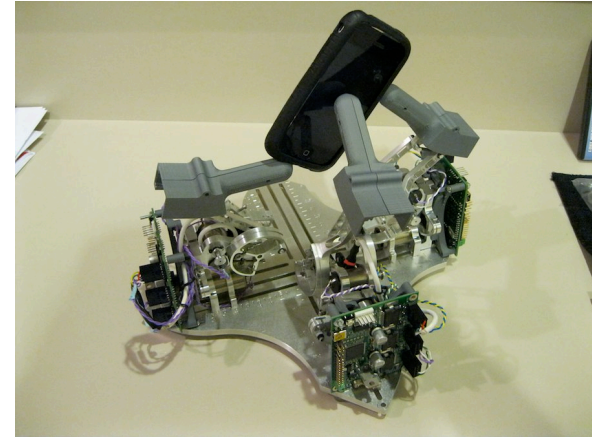


Complex object manipulation with hierarchical optimal control

Dr. Alex Simpkins and
Prof. Emanuel Todorov
University of Washington, Seattle

Object Manipulation

- *Controlling the trajectory or state of an object with external forces applied by manipulators*
- Complex problem
 - Nonlinearities
 - Contacts/collisions
 - Discontinuities
 - Changing problem
 - Friction
 - Redundancy
 - High dimensionality
 - Under-actuation



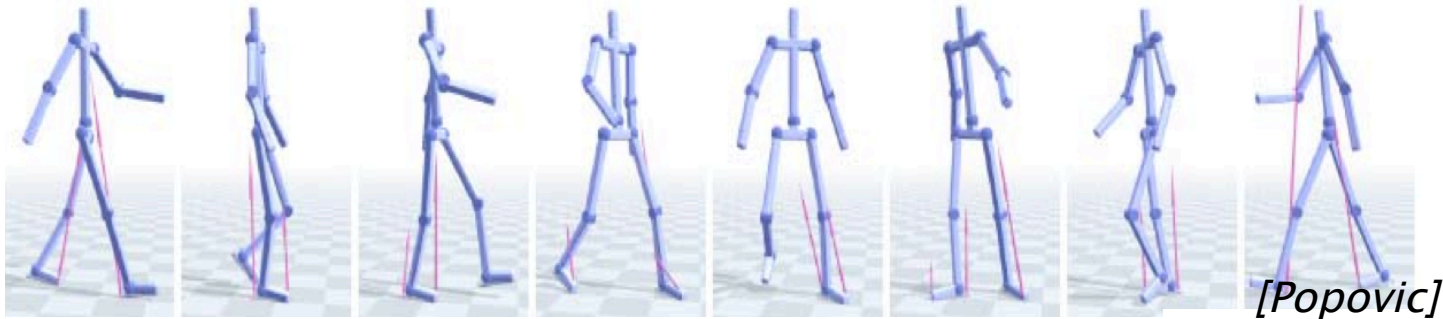
Object Manipulation

▶ Significance/Relevance

- Interaction with the world is part of learning and normal functioning
 - We explore and process Haptic information, expand knowledge
 - Better method, improved learning
- Humans are excellent at interacting dynamically with our dynamic world!
 - This is poorly understood from a control/machine learning perspective
 - Crumple a piece of paper 60 times, you will do it 60 different ways
- Significant portion of neurons in brain involved in sensorimotor processes
- Artificial systems need to interact with the world intelligently



Existing approaches



▶ Manipulation

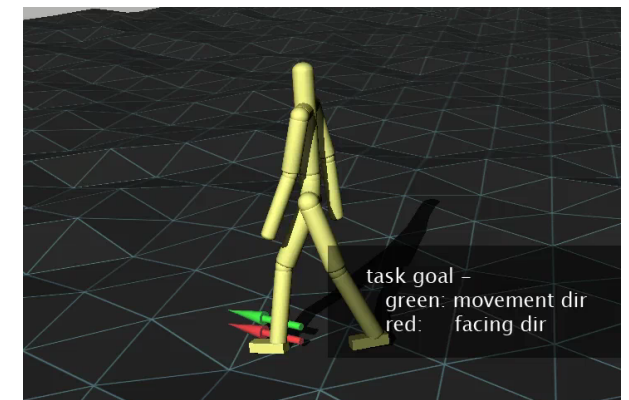
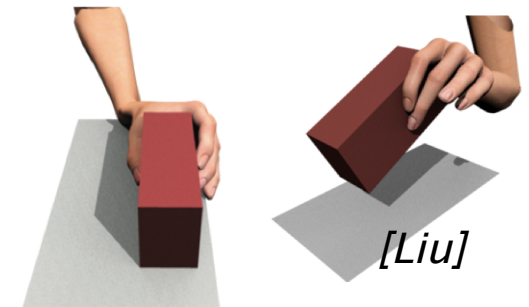
- Assume a grip predefined, contacts static/quasi-static
- Determine forces to move object in prescribed manner
- Optimal control

▶ Grasp studies – how do humans grasp objects?

- Quasi-static notion yet again

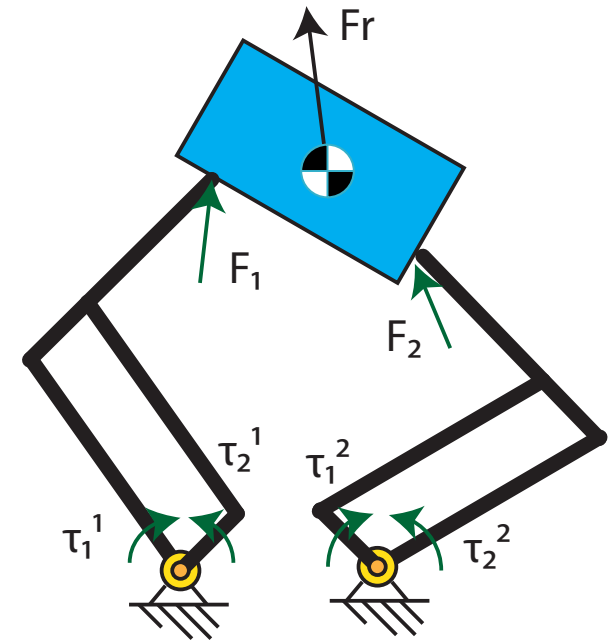
▶ Locomotion approaches

- Manipulation and locomotion are highly related
 - Many of the challenges are similar
- Relevant locomotion approaches which are promising based upon optimal control and RL
 - Typically hierarchical, often offline components



Model

- ▶ 2D – first step
- ▶ Objects
 - Mass, center of mass, inertia, boundary
- ▶ Given # of manipulators
 - Modeled as point masses, since actuators are very capable, and dynamics are approximately linear (dominated by rotor J)
- ▶ Simple/efficient/fast contact/collision algorithm here
 - No-slip condition (equivalent to very sticky objects/manipulator end points)
 - Facilitates realtime implementation
 - Parallel GPU processing possible
- ▶ 2-part computation - total forces on
 - Object
 - Manipulators (contact or not)



$$\sum F_{x,o} = \sum_i f_{x_i} - m_o a_{x,o} \quad (1)$$

$$\sum F_{y,o} = \sum_i f_{y_i} - m_o g - m_o a_{y,o}$$

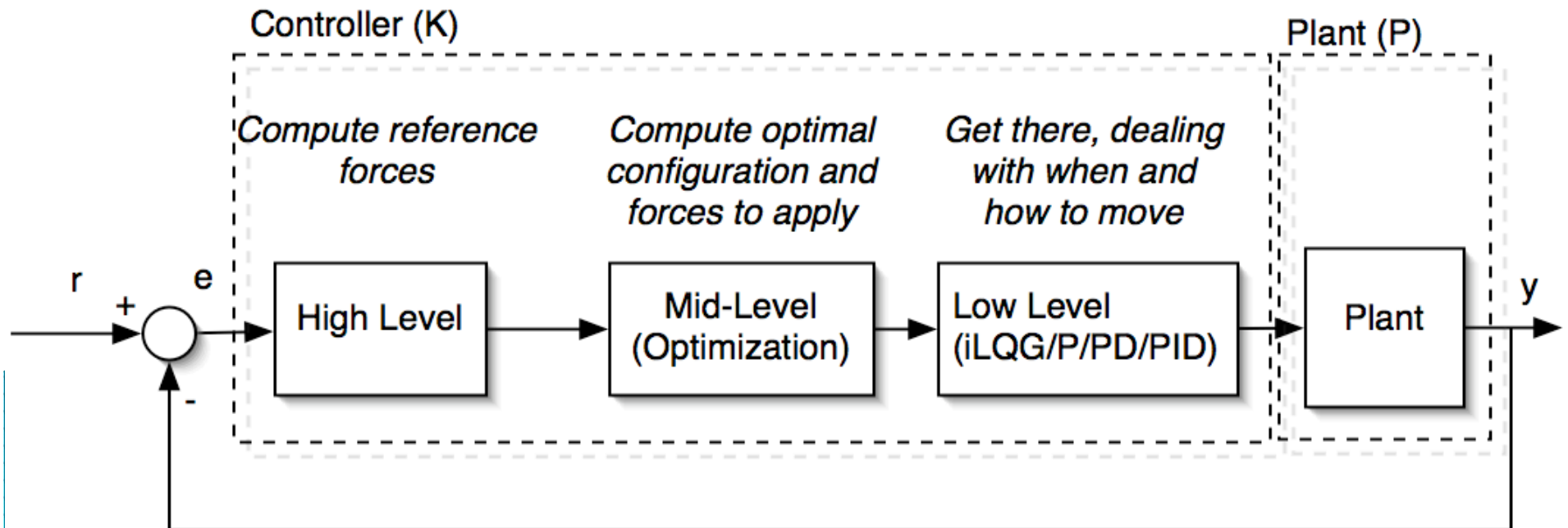
$$\sum M_o = \sum_i (-f_x d_y(\theta) + f_y d_x(\theta))_i - J \ddot{\theta}_o$$

$$a_{x,i} = a_{x,o} + \ddot{\theta}_i d_x(\theta_i)$$

$$a_{y,i} = a_{y,o} + \ddot{\theta}_i d_y(\theta_i)$$

Hierarchical control methodology

- ▶ Break up single complex problem into multiple more tractable problems
- ▶ Hierarchical – allows different strategies at each stage, more freedom
- ▶ Behaviors can be encoded at various levels

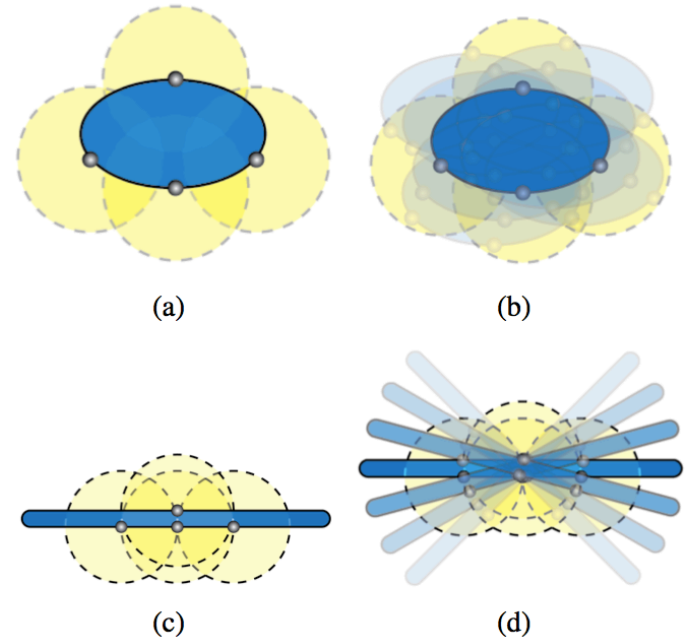


Force-Cost function

$$F_e = K_e \frac{(x - x_c)}{1 + ||x - x_w||^2}$$

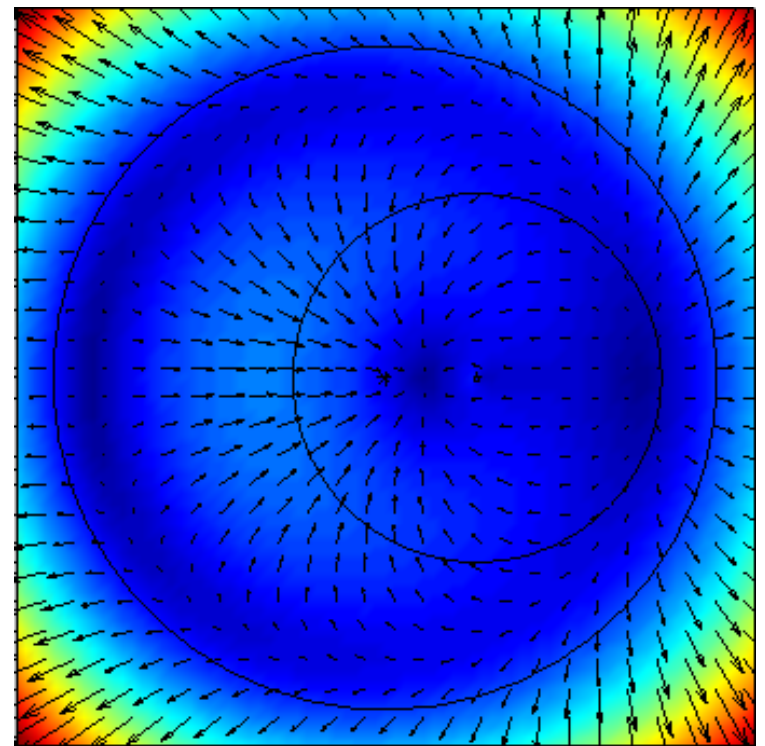
$$F_s = K_s n ||x - x_w|| e^{-a(x-x_c)^2}$$

$$F_t = F_e + F_s$$



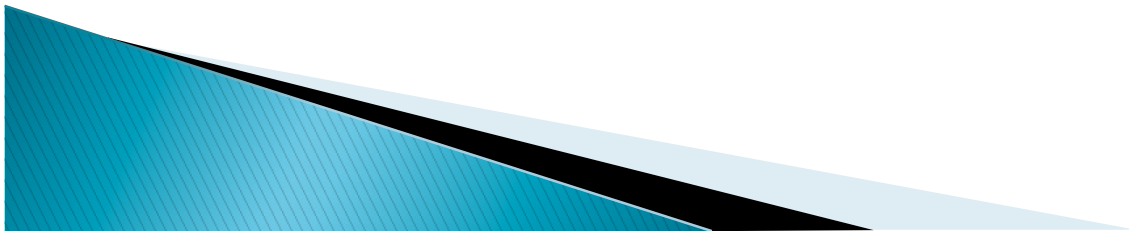
► Mid-Level

- Given required force, and the state of the system
 - What should the individual forces be?
 - Where should they be applied?
- Optimization and FC function
 - Part I : Arranged as quadratic optimization, terms account for
 - Force tracking error
 - Minimizing individual forces
 - Part II : Virtual force field, similar to a cost function
 - State of system, workspace of each manipulator, location of end effector, location and parameters (or estimated) of object

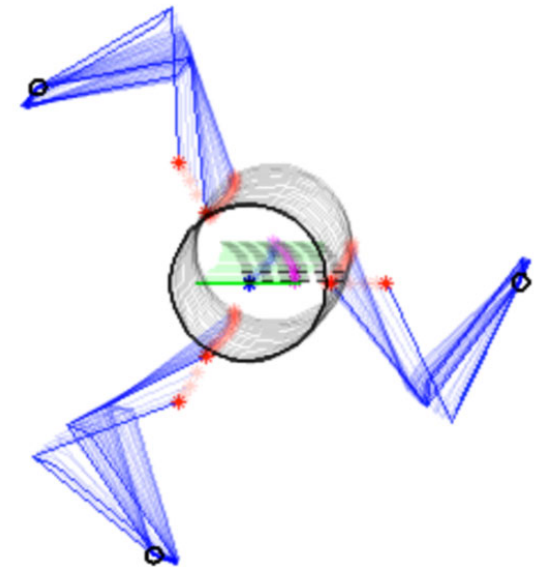
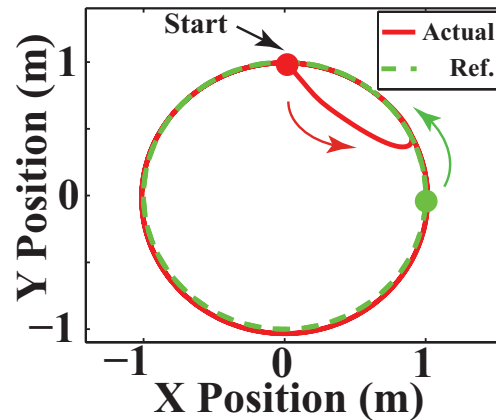
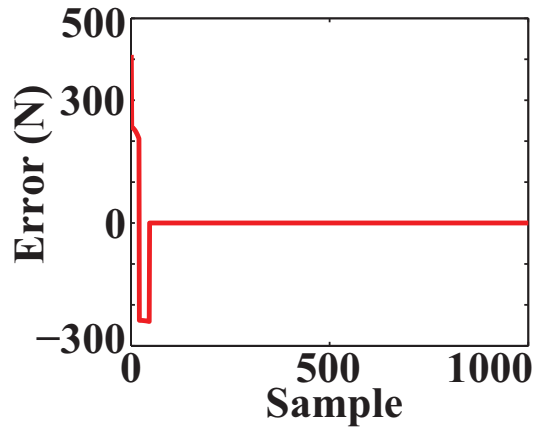
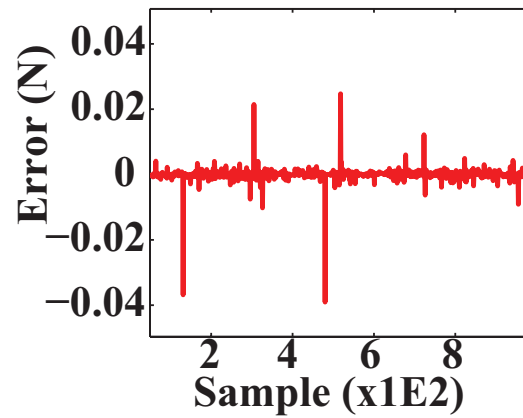
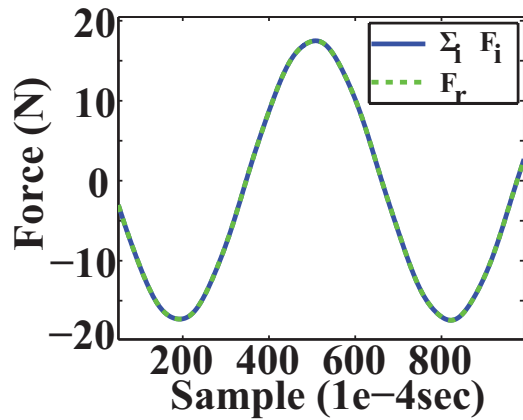


Experimental tasks

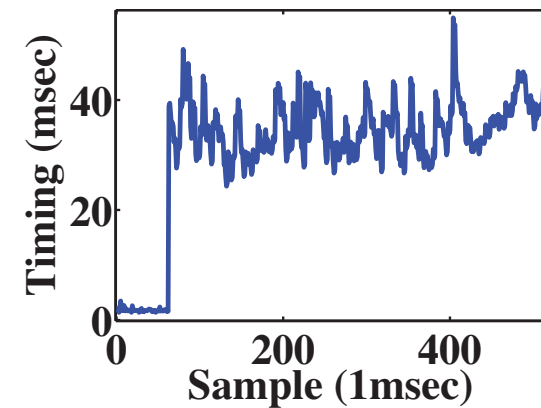
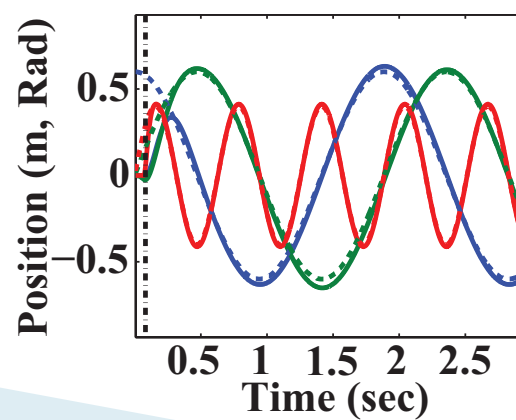
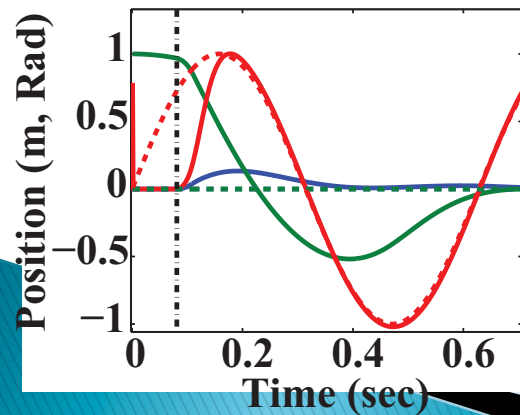
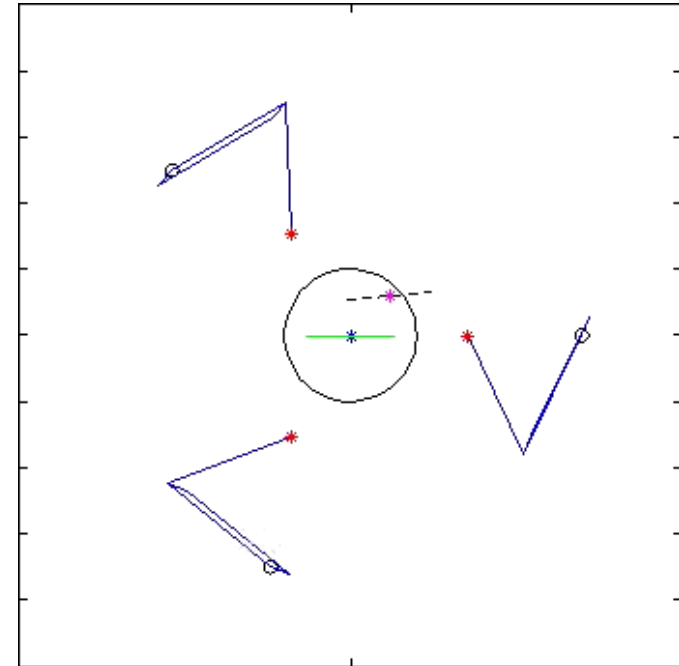
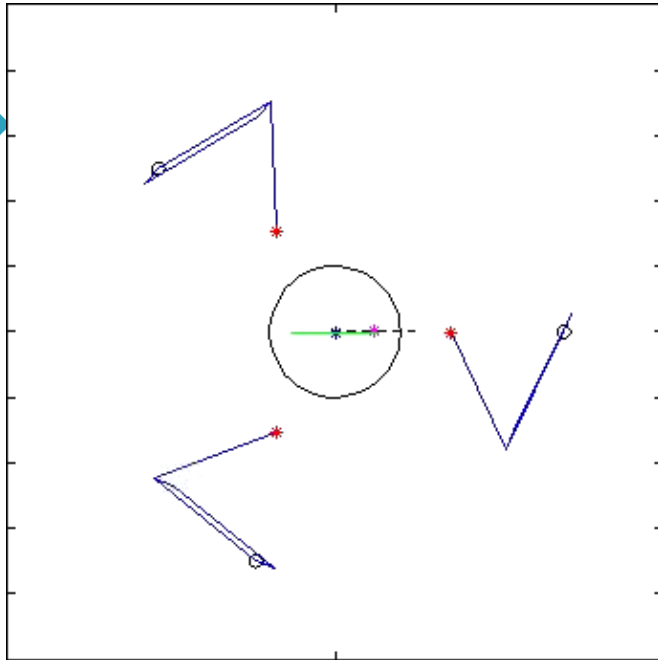
- ▶ Given a # of end effectors, manipulate an object of known parameters
 - Grab object, then track some reference for the object
 - Perform continuous rotation of the object in place
 - In both cases manipulator bases are fixed
 - Everything happens due to manipulators, not an arm



Results – force tracking



Results – grasp and track



Conclusions

▶ Contributions

- New dynamic hierarchical control approach to manipulation, also applicable to locomotion
- Minimal manual tweaking (as opposed to some 'painful' methods), tuned with intuitive parameters (only a few), easy to expand behavioral complexity or blend/change behaviors online
- Realtime implementation – no offline computation, fast enough to run on real robots
- Manipulation and locomotion treated as the same problem
- Joint limit handling with soft boundary acting as a spring when moving outside workspace, contributes to numerical stability, smoothness, parallels biological systems

▶ In progress/next steps

- 3D
- Implementation on real robots (object spinning task)
- MPC at lower level vs. force fields (comparison)
- Stability/robustness analysis more quantitative
- Active sensing – learn object while manipulating, or manipulate to learn object
- Compare with trajectory methods, also being developed in our lab





Thank you

*More information at
casimpkinsjr.radiantdolphinpress.com*

Appendix – 1

- ▶ Ease of tuning – high level doesn't affect low level stability
 - Build stable system in pieces if necessary with difficult systems

